

An interval ordering data type is based on an interval-ordering relation  $P$ : for any  $a, b, c, d \in A$ ,

1.  $P(a, a)$ ,
2.  $P(a, b) \& P(c, d) \Rightarrow (P(a, d) \vee P(c, b))$ .

It is proved in [Fishbern, 1970] that a numeric representation for  $\langle A, P \rangle$  exists completely consistent with properties 1 and 2. There are functions  $U$  and  $S$ ,  $U, S: A \rightarrow \mathbb{R}^+$ , such that for any  $a, b \in A$ ,

$$P(a, b) \Leftrightarrow U(a) + S(a) < U(b).$$